Discussion: "Strategic Trading and Manipulation in Trade at Settlement Contracts"

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- Multi-period rational expectations equilibrium model of trading like Admati-Pfleiderer (1988)
- $\bullet\,$ Three periods: $T_1,\,T_S,\,T_2.$ Risk-neutral market maker sets prices to expectation of asset value cond. order flow
- Each period, short-lived informed traders and noise traders
- N_d TAS market makers:
 - Receives TAS order flow F^d (i.e. commits to sell wheat futures at Tuesday settle)
 - \bullet Wants to net 0, so needs to buy $-F^d$ futures across $T_1,\,T_S,\,T_2$
 - Profits:

$$\Pi_{d} = E_{d} \left[F^{d} \left[-\varphi_{1} P_{1} + (1-\varphi_{s}) P_{s} + (1-\varphi_{1}-\varphi_{s}) P_{2} \right] \right]$$

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- ⇒ I might want to buy more than 3 wheat futures on Mon and Tues! Sell the extra on Wed after Tuesday's settle
- Futures markets can't tell whether I'm informed or not, so may have partially permanent price impact

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- Over-trading happens more when market is concentrated: few dealers, large colluding block of dealers, or probabilistically concentrated markets
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- Aside: manipulation is an interesting case where concentration leads to more, not less, trading!
 - \bullet Classic models: more concentration \implies more price impact \implies $\underline{{\sf less}}$ aggressive trading
 - (Some) manipulation models: more concentration ⇒ more price impact, more influence on TAS profits ⇒ more aggressive trading!

Cool paper! Two main comments:

- What's the role of correlated shocks across TAS dealers in the model?
- (Speculative) Is there any clean benchmark for "obviously non-manipulative" trading for TAS contracts?

- What does the assumption of correlated shocks to TAS market maker inventory give us?
- My current understanding: largely a modelling device, so that their order flow sums to something that doesn't go to 0? I was a bit confused
- Irrelevant for 1 TAS dealer, hence can't be driving the results
- What's the comparative static? Is over-trading more or less prevalent when shocks are more correlated?

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 - Buy 3 contracts immediately at time 0?
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- None of these are riskless, and none "obviously" correct!

Should all trading happen before T_s ?

• What about trading very close to settlement?

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- What if we bought 3 contracts exactly at T_s , just before settlement?
- But if there was more buying earlier, in T_1 , is that manipulation?
- $\bullet\,$ If we buy 3 contracts exactly at $T_s,$ can't actually profit from this manipulation!

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- $\bullet\,$ If we buy 3 contracts exactly at $T_s,$ can't actually profit from this manipulation!
- \bullet Also not obvious to me, across broader class of models, that in a competitive world there's no buying after $T_{\rm s}$
 - If goal is "spread out price impact", buying late could be as good as buying early
 - But buying late can't affect settlement prices
- "Overtrading" seems clearly bad, but is there stuff we can say is obviously "not bad"?

- Expositional: might be good to explicitly say underlying futures market maker is "competitive" and sets prices to conditional expectations (since the TAS market makers aren't)
- For extension work, seems potentially interesting to incorporate risk aversion